

**Peter McKenzie Armstrong**

# **Pitch/Time Swaps**

**as applied to the Fugue subjects of  
J.S. Bach's *Das Wohltemperierte Klavier***

**scored for solo piano**

**Op. 39, 2nd Ed.**

*Edition Ottaviano Petrucci*

# NOTES

## GENERATION

Encoded as an X/Y dot graph, rotated 90 degrees, then read in that position left-to-right, musical scoring is seen with its essential parameters exchanged, pitch indications having become instead relative attack times and vice versa. With the rotation anticlockwise (as in these examples), pitchwise top/bottom translate to timewise first/last, etc.

I have applied this procedure to the Fugue subjects of J.S. Bach's *Das Wohltemperierte Klavier*, trusting that juxtaposition of such originals (linear only) and their rotations (mainly chordal) may enhance its promise as a compositional option.

As used here, the rotation addresses its source's sounding notes only (not also rests) and without subsequent reportioning of the results (as with many integral-serialist algorithms). For a representative graph see Appendix A.

## RE "X/Y->Y/X" SECTIONS:

### NOTATION

- Notehead colors: green, the original's recurrent pitches; red, the rotation's corresponding simultaneities; grey, exceptions (applying in both senses).
- Accidentals (default '#' in their generating graph) are respelled in their score as appears harmonically and voice-leading-wise most plausible.
- Meter signatures and articulation markings are chosen post-process as best to convey emergent patterns.

### PERFORMANCE

- Accidentals apply once only, c/o LilyPond's style "forget".
- Tied anticipations, unless slashed, are to occur on-beat.
- Legato connection is intended only within slurs, not also from their final note.
- Damper pedal use is expected for realizing slurs where necessary, or for enhancing immediate resonance, but not for connecting non-slurred notes.
- I suggest programming as a selection of perhaps six of these pages with their order, tempi, dynamics and hand distributions at player's discretion.

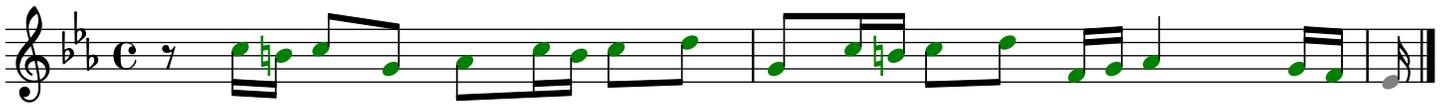
### MISCELLANY

- WTC I:19 - I have extended this quoted subject a full bar beyond its answer's entry.
- WTC I:24 - Source pitches recurring only in embellishment are not counted for rotation.
- WTC II:10 is the only subject rotated in separate sections; its length otherwise forces unworkably overstacked chords.
- Rotating fugue subjects alone presents only recurrence->simultaneity. For an example addressing also the reverse, see Appendix B.
- Suggested articulations for performance of the fugue subjects per se are listed in Appendix C. I do not claim that these are original with me, though I expect some are. Their listing is separated from the main score, as performance issues in the source were not factors in the parameter-swapping as conceived.

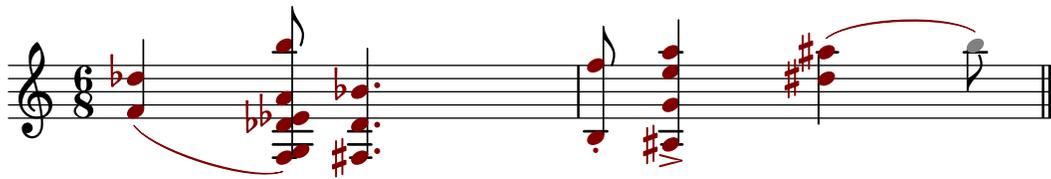


2

WTC I: 2 (BWV 847)



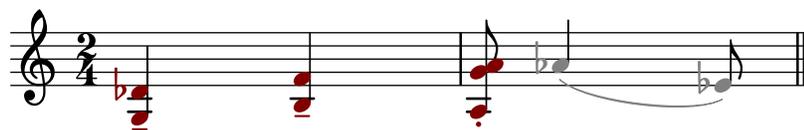
X/Y->Y/X



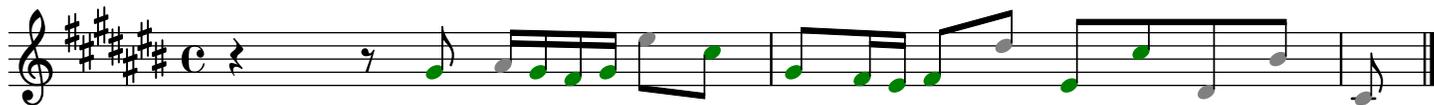
WTC II: 2 (BWV 871)



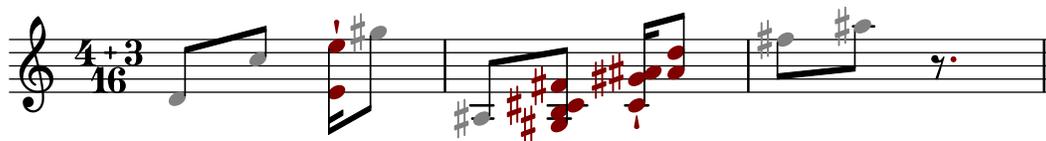
X/Y->Y/X



## WTC I: 3 (BWV 848)



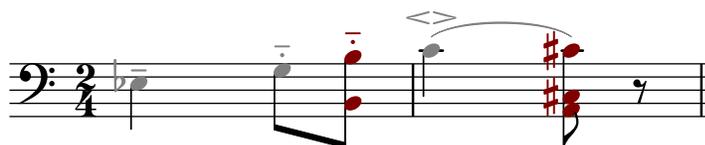
## X/Y-&gt;Y/X



## WTC II: 3 (BWV 872)



## X/Y-&gt;Y/X

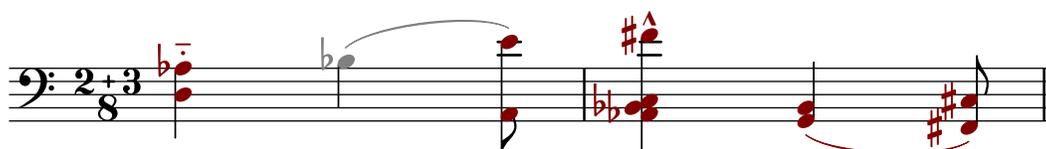




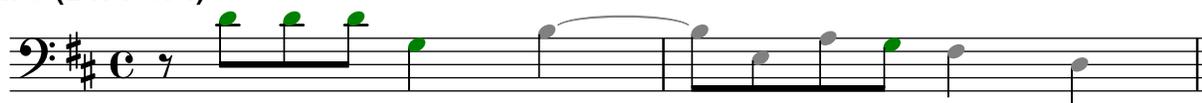
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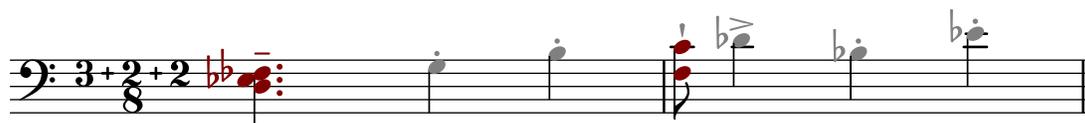
## X/Y-&gt;Y/X



## WTC II: 5 (BWV 874)

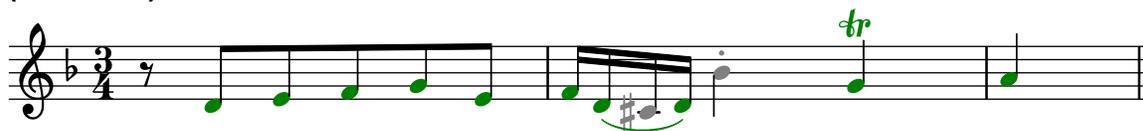


## X/Y-&gt;Y/X

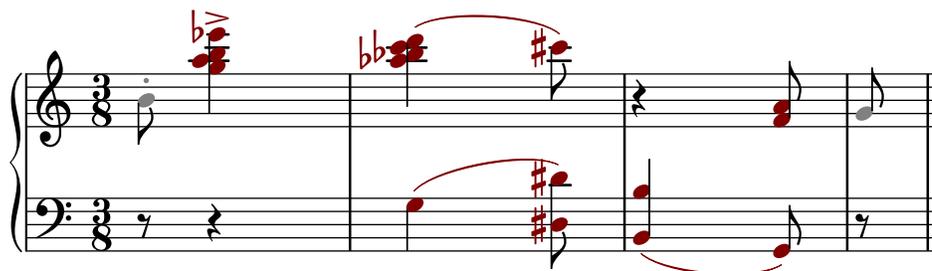


6

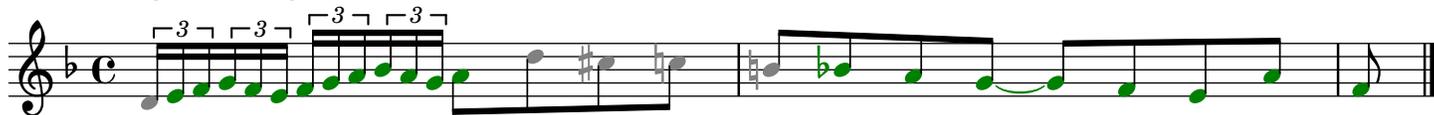
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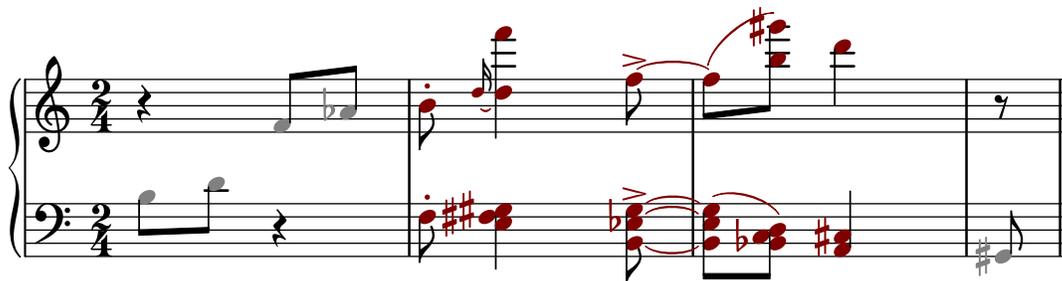
X/Y->Y/X



WTC II: 6 (BWV 875)



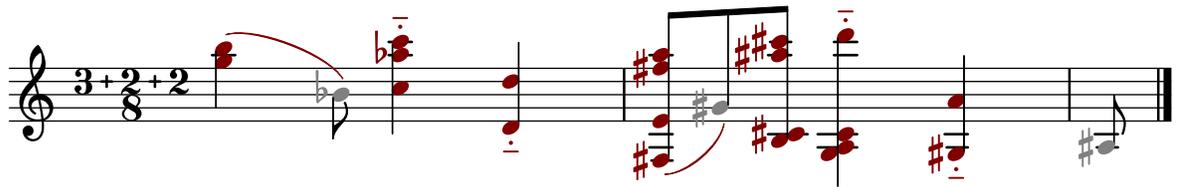
X/Y->Y/X



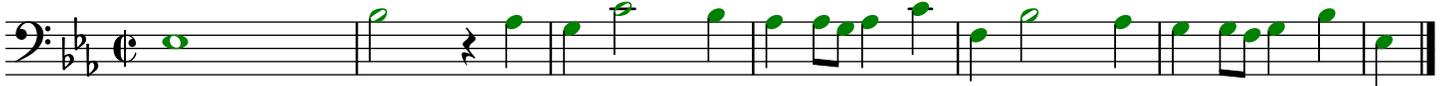
## WTC I: 7 (BWV 852)



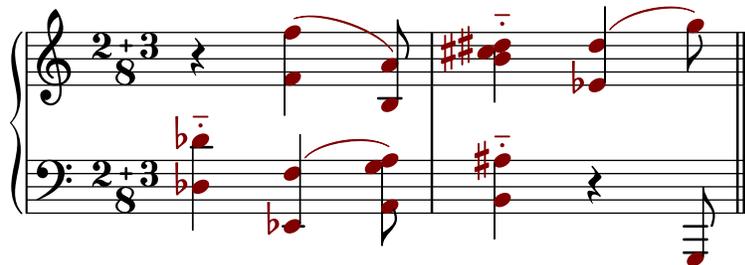
## X/Y-&gt;Y/X



## WTC II: 7 (BWV 876)

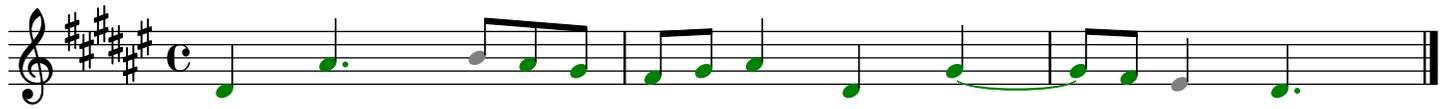


## X/Y-&gt;Y/X

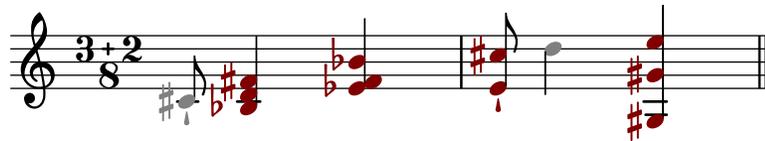


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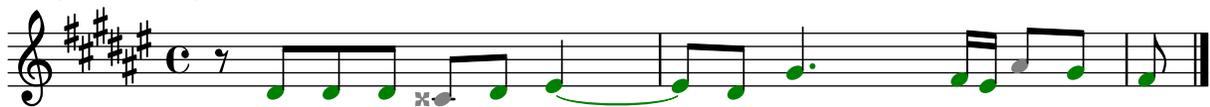
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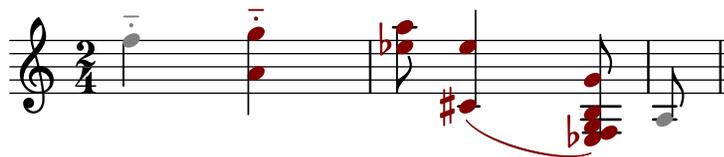
X/Y->Y/X



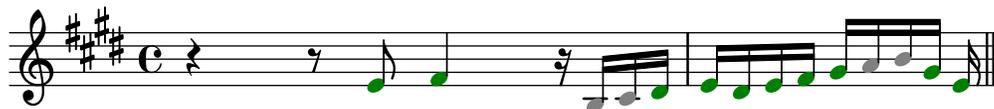
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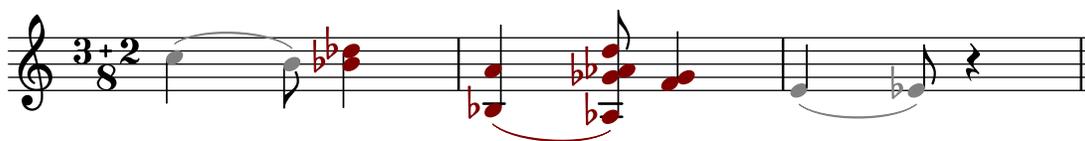
X/Y->Y/X



## WTC I: 9 (BWV 854)



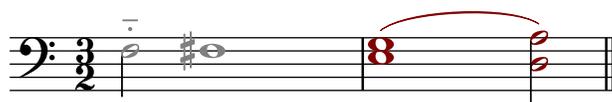
## X/Y-&gt;Y/X



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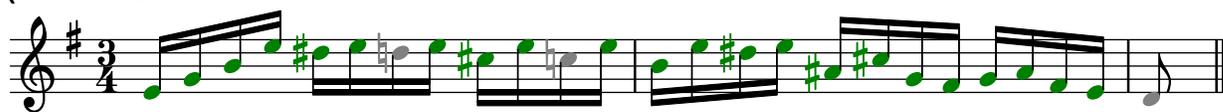


## X/Y-&gt;Y/X

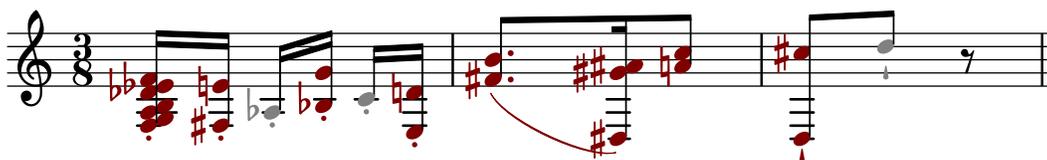


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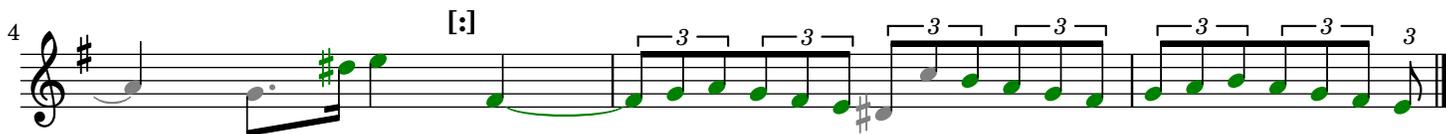
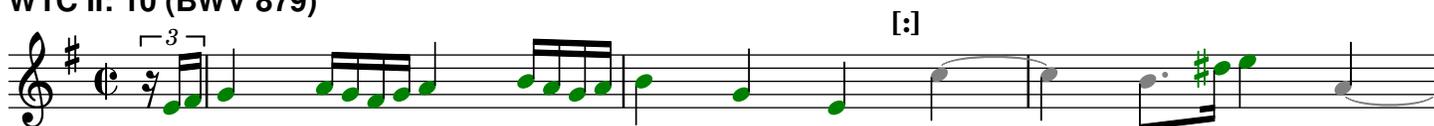
WTC I: 10 (BWV 855)



X/Y->Y/X



WTC II: 10 (BWV 879)



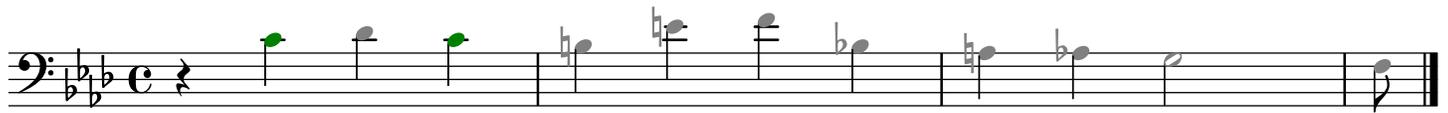
X/Y->Y/X



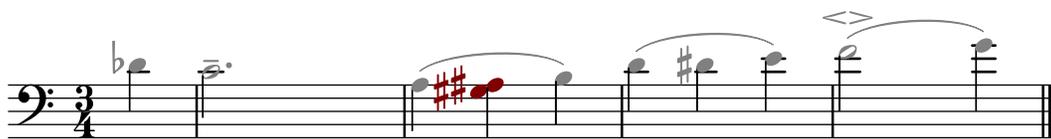


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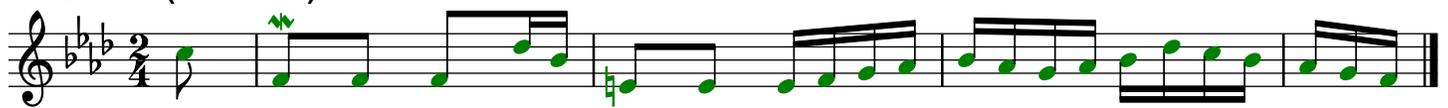
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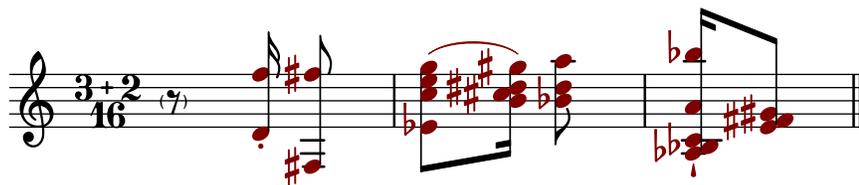
X/Y->Y/X



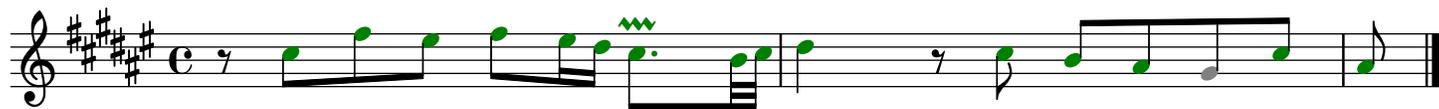
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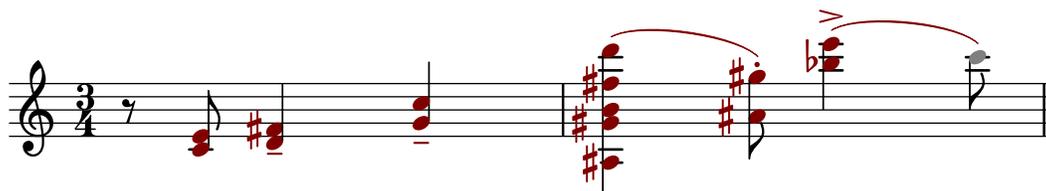
X/Y->Y/X



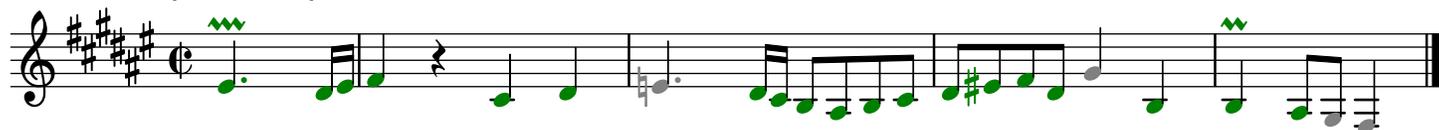
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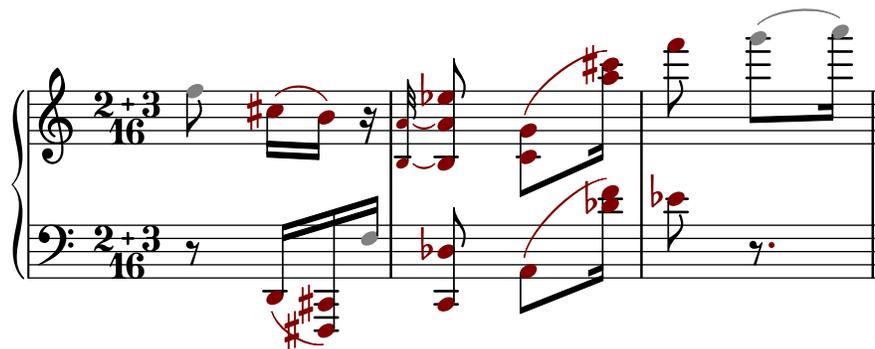
X/Y->Y/X



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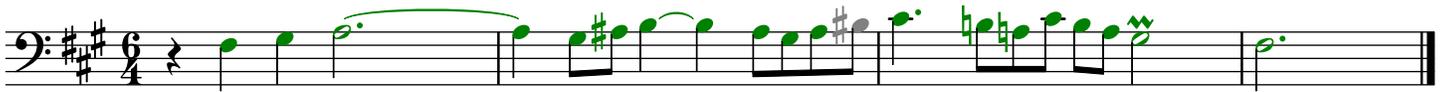


X/Y->Y/X

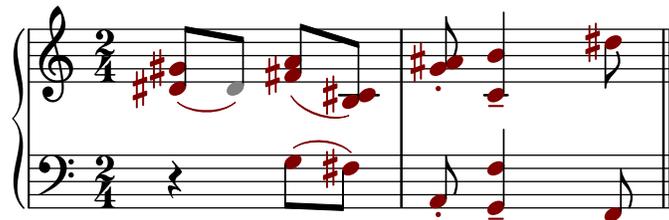


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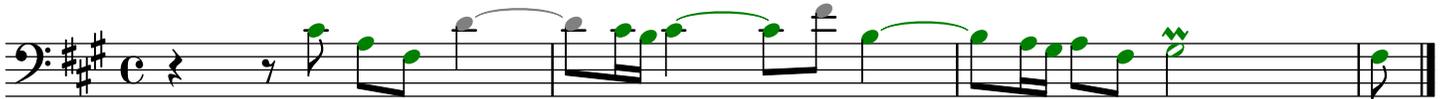
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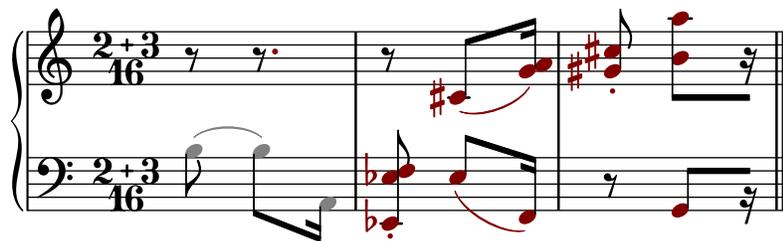
X/Y->Y/X



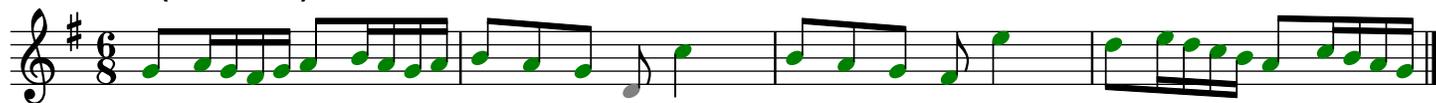
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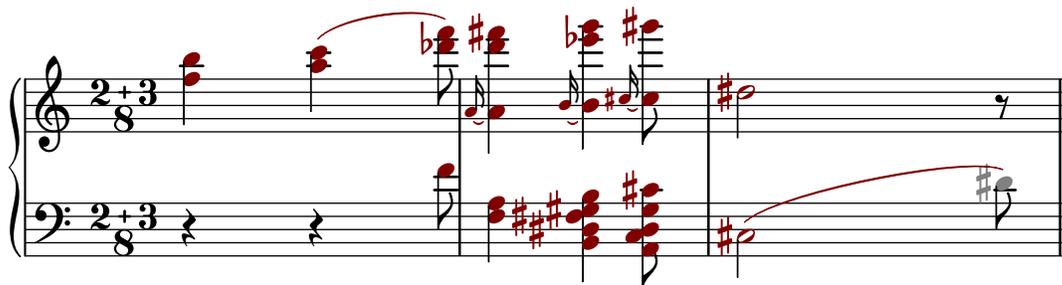
X/Y->Y/X



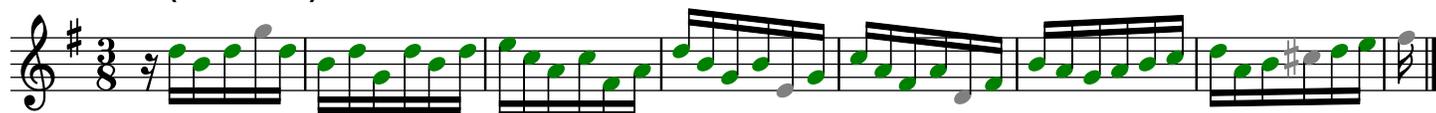
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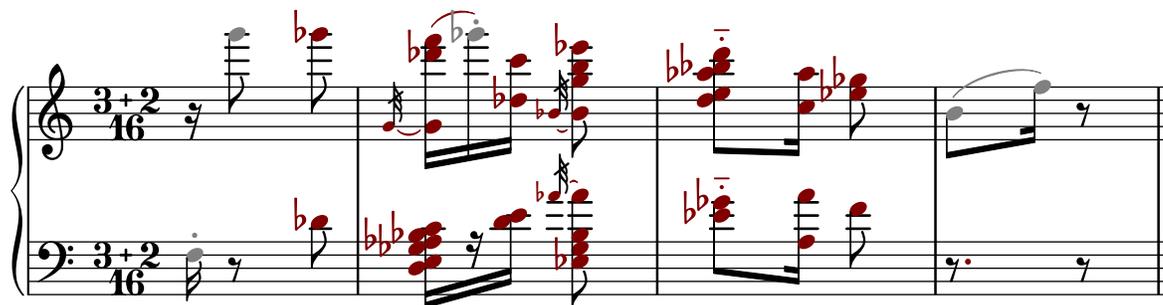
X/Y->Y/X



WTC II: 15 (BWV 884)



X/Y->Y/X

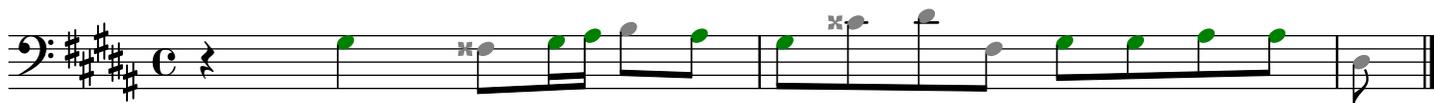




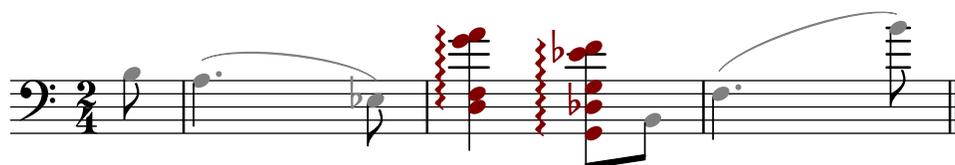


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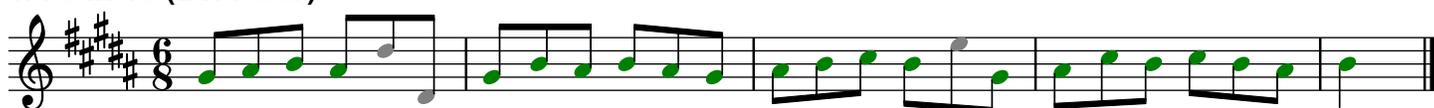
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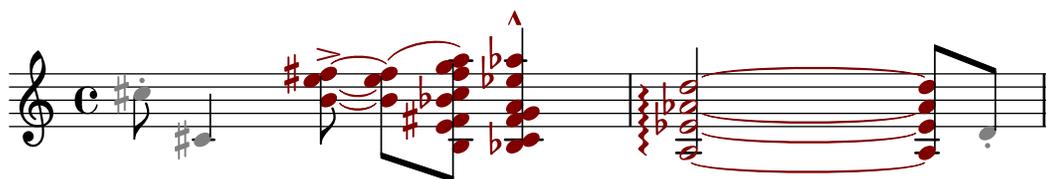
X/Y->Y/X



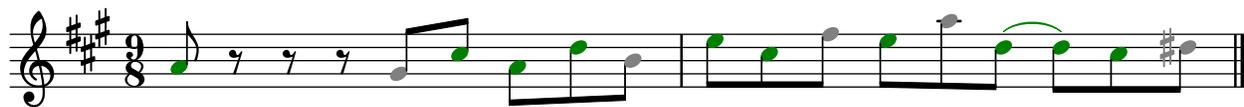
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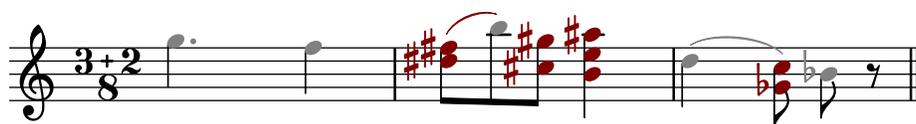
X/Y->Y/X



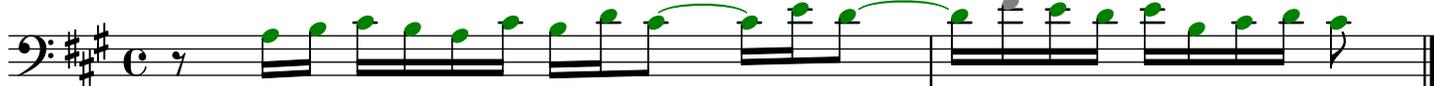
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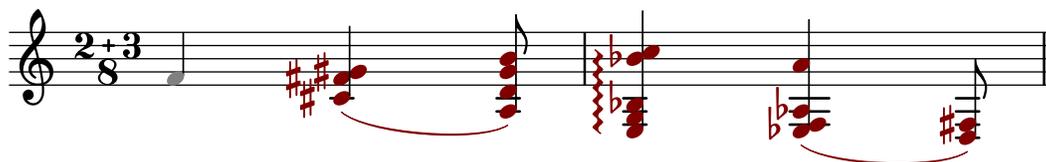
## X/Y-&gt;Y/X



## WTC II: 19 (BWV 888)

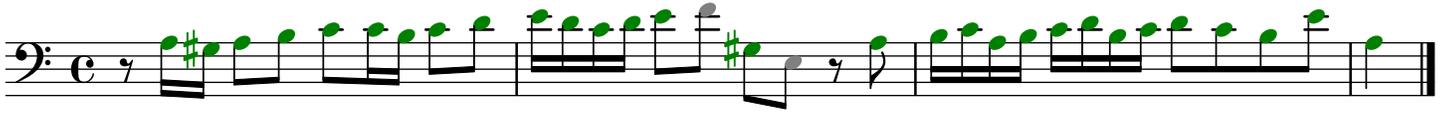


## X/Y-&gt;Y/X

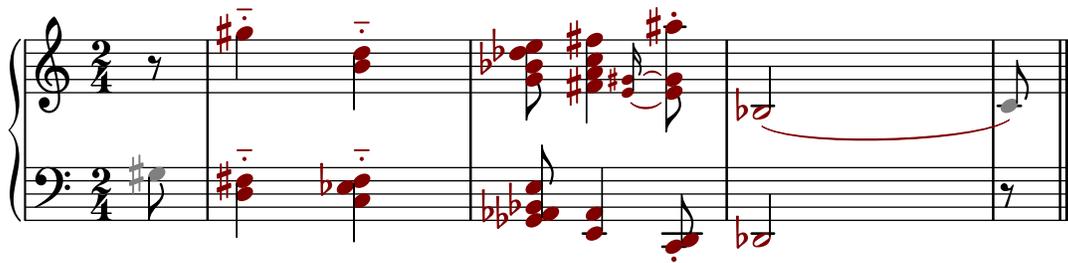


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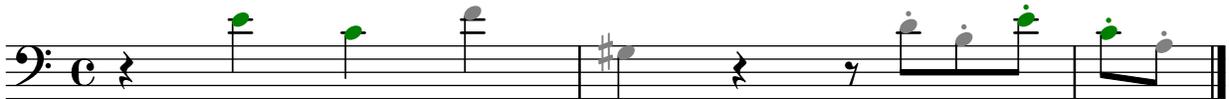
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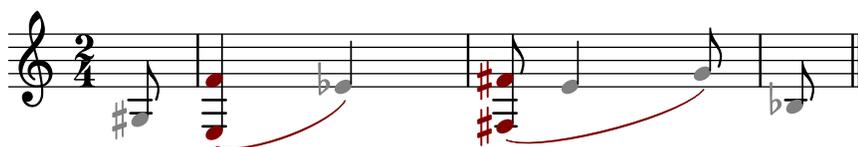
X/Y->Y/X



WTC II: 20 (BWV 889)



X/Y->Y/X





22

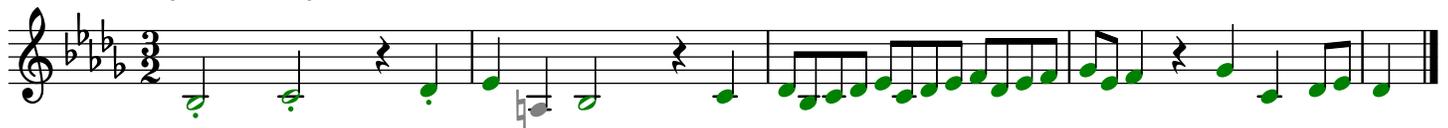
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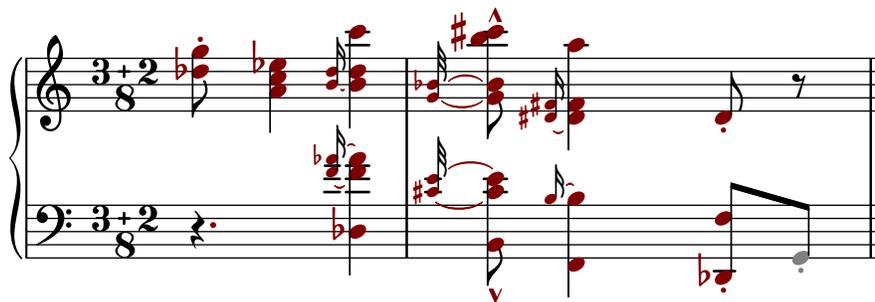
X/Y->Y/X



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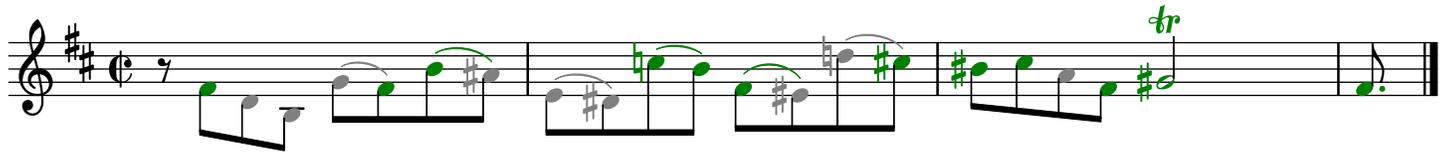
X/Y->Y/X



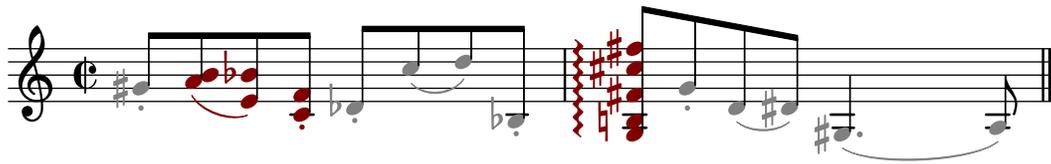


24

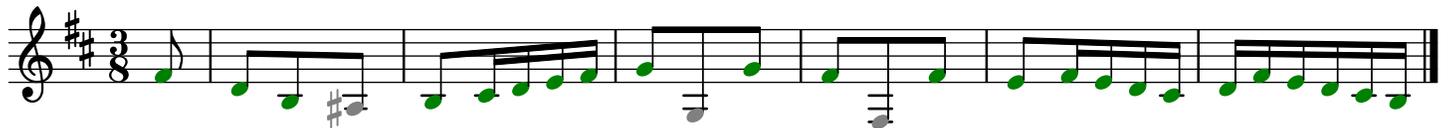
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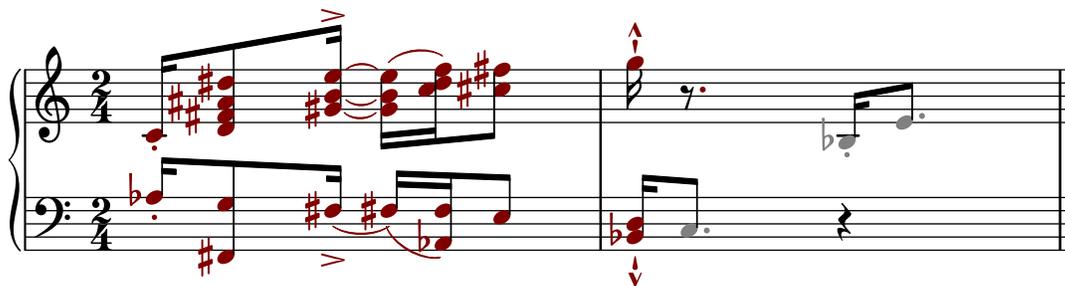
X/Y->Y/X



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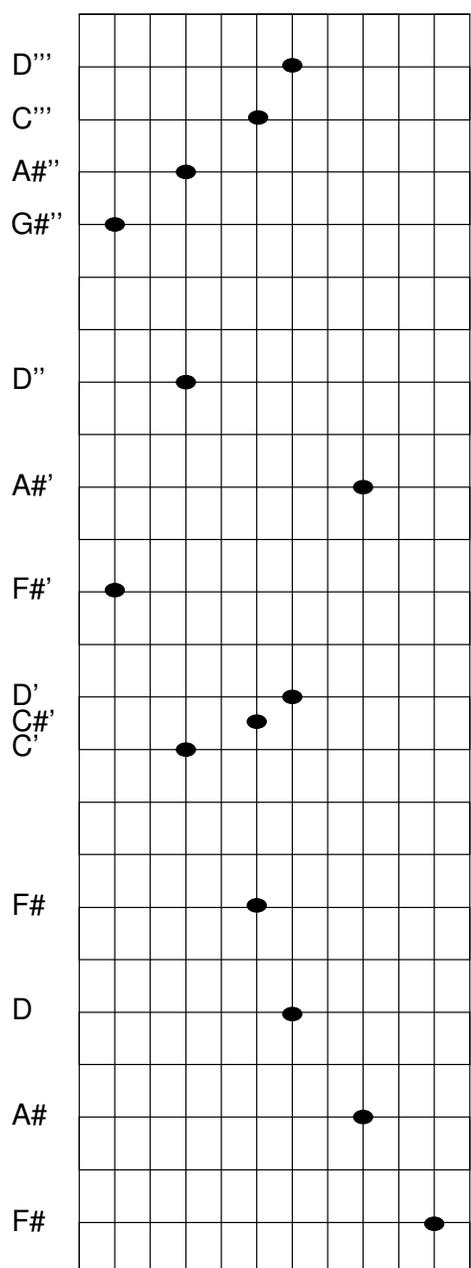
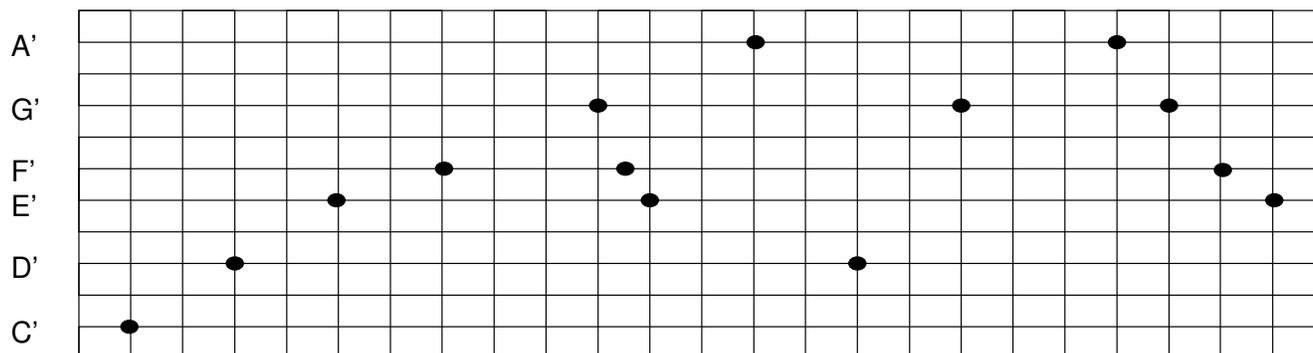


X/Y->Y/X



# Appendix A \*

## Rotation-Graph Example



### ABOVE: WTC I:1 (BWV 846), Fugue Subject

Generally these vertical/horizontal grid units match their source's minimum interval/duration. Exceptions, such as this example's offline F', will not affect their note's scored proportions.

Octave level is per LilyPond's notation.

### OPPOSITE: X/Y->Y/X, 90 Deg ACW Rotation

Accidentals (all '#' here by default) are due for probable respelling in score.

The shortest source duration translates by default to a semitone, and vice versa. If that duration is contextually especially short, as here, wholetones will become the sounding intervallic unit.)

Output pitch center is chosen to close-match that of the source.

\* This page was generated in Xfig 3.2.8.

# Appendix B

J.S. Bach, Chorale "Meine Seel' erhebt den Herren", BWV 324

The first system of musical notation for the chorale. It consists of two staves: a treble clef staff on top and a bass clef staff on the bottom. The key signature is two flats (B-flat and E-flat), and the time signature is common time (C). The music is written in a simple, homophonic style with chords and single notes. The first measure has a whole note chord in the treble and a half note chord in the bass. The second measure has a quarter note chord in the treble and a quarter note chord in the bass. The third measure has a quarter note chord in the treble and a quarter note chord in the bass. The fourth measure has a quarter note chord in the treble and a quarter note chord in the bass. The fifth measure has a quarter note chord in the treble and a quarter note chord in the bass. The sixth measure has a quarter note chord in the treble and a quarter note chord in the bass. The system ends with a double bar line and repeat dots.

The second system of musical notation for the chorale. It consists of two staves: a treble clef staff on top and a bass clef staff on the bottom. The key signature is two flats (B-flat and E-flat), and the time signature is common time (C). The music is written in a simple, homophonic style with chords and single notes. The first measure has a whole note chord in the treble and a half note chord in the bass. The second measure has a quarter note chord in the treble and a quarter note chord in the bass. The third measure has a quarter note chord in the treble and a quarter note chord in the bass. The fourth measure has a quarter note chord in the treble and a quarter note chord in the bass. The fifth measure has a quarter note chord in the treble and a quarter note chord in the bass. The sixth measure has a quarter note chord in the treble and a quarter note chord in the bass. The system ends with a double bar line and repeat dots.

The third system of musical notation for the chorale. It consists of two staves: a treble clef staff on top and a bass clef staff on the bottom. The key signature is two flats (B-flat and E-flat), and the time signature is common time (C). The music is written in a simple, homophonic style with chords and single notes. The first measure has a whole note chord in the treble and a half note chord in the bass. The second measure has a quarter note chord in the treble and a quarter note chord in the bass. The third measure has a quarter note chord in the treble and a quarter note chord in the bass. The fourth measure has a quarter note chord in the treble and a quarter note chord in the bass. The fifth measure has a quarter note chord in the treble and a quarter note chord in the bass. The sixth measure has a quarter note chord in the treble and a quarter note chord in the bass. The system ends with a double bar line and repeat dots.

The fourth system of musical notation for the chorale. It consists of two staves: a treble clef staff on top and a bass clef staff on the bottom. The key signature is two flats (B-flat and E-flat), and the time signature is common time (C). The music is written in a simple, homophonic style with chords and single notes. The first measure has a whole note chord in the treble and a half note chord in the bass. The second measure has a quarter note chord in the treble and a quarter note chord in the bass. The third measure has a quarter note chord in the treble and a quarter note chord in the bass. The fourth measure has a quarter note chord in the treble and a quarter note chord in the bass. The fifth measure has a quarter note chord in the treble and a quarter note chord in the bass. The sixth measure has a quarter note chord in the treble and a quarter note chord in the bass. The system ends with a double bar line and repeat dots.

The fifth system of musical notation for the chorale. It consists of two staves: a treble clef staff on top and a bass clef staff on the bottom. The key signature is two flats (B-flat and E-flat), and the time signature is common time (C). The music is written in a simple, homophonic style with chords and single notes. The first measure has a whole note chord in the treble and a half note chord in the bass. The second measure has a quarter note chord in the treble and a quarter note chord in the bass. The third measure has a quarter note chord in the treble and a quarter note chord in the bass. The fourth measure has a quarter note chord in the treble and a quarter note chord in the bass. The fifth measure has a quarter note chord in the treble and a quarter note chord in the bass. The sixth measure has a quarter note chord in the treble and a quarter note chord in the bass. The system ends with a double bar line and repeat dots.

### Rotation: Exchange of Pitch/Time Proportions applied to the chorale phrases separately

S\*.....  
A.....  
T.....  
B.....

S.....  
A.....  
T.....  
B.....

S.....  
A.....  
T.....  
B.....

S.....  
A.....  
T.....  
B.....

(T).....  
(B).....

\* Dotted lines indicate corresponding chorale voice ranges, with the left-most event here referencing the top-most chorale pitch.

## Appendix C

### Suggested Fugue-Subject Articulations \*

with the goal to clarify pattern

#### WTC I: 1 (BWV 846)



#### WTC II: 1 (BWV 870)



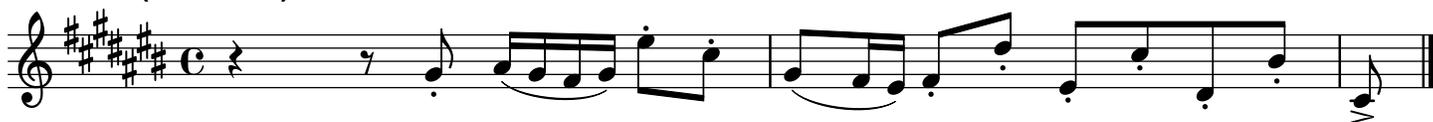
#### WTC I: 2 (BWV 847)



#### WTC II: 2 (BWV 871)



#### WTC I: 3 (BWV 848)



#### WTC II: 3 (BWV 872)



\* The few in Bach's hand (according to G. Henle Verlag) are printed here in red.

## WTC I: 4 (BWV 849)



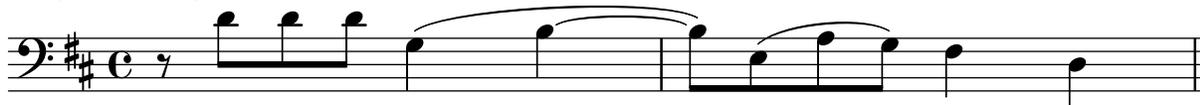
## WTC II: 4 (BWV 873)



## WTC I: 5 (BWV 850)



## WTC II: 5 (BWV 874)



## WTC I: 6 (BWV 851)



## WTC II: 6 (BWV 875)



## WTC I: 7 (BWV 852)



## WTC II: 7 (BWV 876)



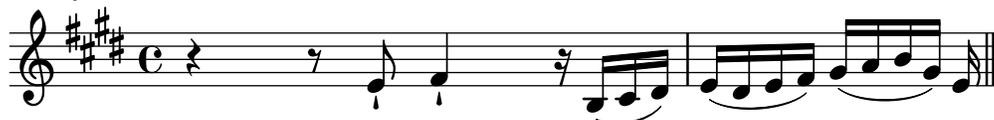
## WTC I: 8 (BWV 853)



## WTC II: 8 (BWV 877)



## WTC I: 9 (BWV 854)



## WTC II: 9 (BWV 878)





## WTC I: 13 (BWV 858)



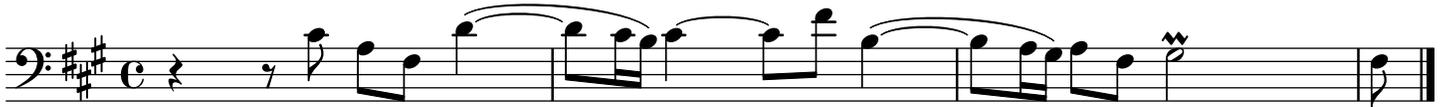
## WTC II: 13 (BWV 882)



## WTC I: 14 (BWV 859)



## WTC II: 14 (BWV 883)



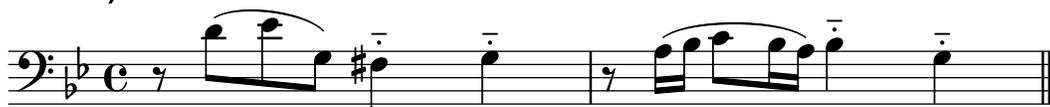
## WTC I: 15 (BWV 860)



## WTC II: 15 (BWV 884)



## WTC I: 16 (BWV 861)



## WTC II: 16 (BWV 885)



## WTC I: 17 (BWV 862)



## WTC II: 17 (BWV 886)



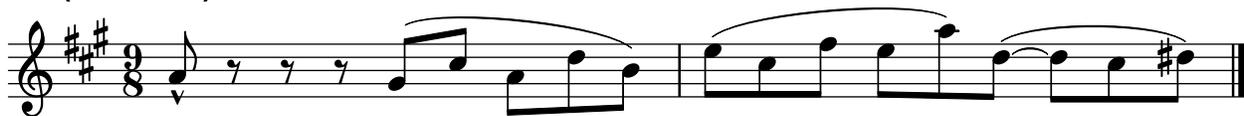
## WTC I: 18 (BWV 863)



## WTC II: 18 (BWV 887)



## WTC I: 19 (BWV 864)



## WTC II: 19 (BWV 888)



## WTC I: 20 (BWV 865)



## WTC II: 20 (BWV 889)



## WTC I: 21 (BWV 866)



## WTC II: 21 (BWV 890)



## WTC I: 22 (BWV 867)



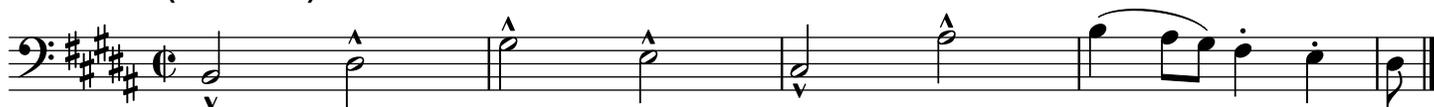
## WTC II: 22 (BWV 891)



## WTC I: 23 (BWV 868)



## WTC II: 23 (BWV 892)



## WTC I: 24 (BWV 869)



## WTC II: 24 (BWV 893)

